

Studies on Memristor Characterization based on Non-linear Dopant Drift Model Modeled with Window function

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Abstract.

In the age of information and communication, information storage with the capability of non-volatile low power has attracted considerable interest. Memristive devices focus on these attributes and were achieved using nanotechnology. However, to design circuits with these memristive devices, the characteristic needs to be described by a mathematical model. Many models such as linear ion-drift model, non-linear ion-drift model, Threshold Adaptive Memristor (TEAM) model have been proposed. These models should resemble the physical devices and also compute efficiently. In the present paper, the characterization of memristor based on SPICE non-linear dopant drift model focusing on various parametric results to achieve better i-v characteristics and power consumption compared with linear ion drift model.

INTRODUCTION

Memristor forms the fourth fundamental passive element defined as "memory resistor" theoretically proposed by Chua[1]. The elementary circuit passive elements such as inductor, capacitor, resistor and memristor are related to each other as shown in fig. 1. When memristive devices switched from an high resistive state to low resistive state when power is applied and retains its state even though the power removed from the device thus an potential candidate for non-volatile information storage applications. Furthermore, the original high resistive state is switched from low resistive state by application of reverse polarity voltage thus behaving as threshold type switching. It has been observed experimentally in chalcogenide materials[2,3] also exhibiting threshold switching. The pinched hysteresis loop depends on the frequency of the applied voltage which is an inherent characteristics of the memristor[4]. Various application on memristor are neural networks, analog circuits, memcapacitive, meminductive and chaotic circuits for communication [5,6,7,8]. In the present work an spice model simulation based on non-linear dopant drift model to characterize the memristive devices mainly focusing on various parametric analysis results namely (i) effect of the variation in frequency with fixed applied voltage, (ii) effect of the amplitude of the applied voltage, (iii) effect of the thickness of the bilayer structure, (iv) variation of ionic mobility and power dissipation to achieve better v-i characteristics which would aid in physical fabrication of memristor devices. Furthermore, to implement synapse (to connect between two neurons) power consumption must be low. To simulate brain requires Tera Bytes of computer memory, however with memristor low power consumption is possible. Hence, power dissipation to study and simulate memristor non-linear dopant drift with linear-ion drift model are compared.

NON-LINEAR ION DOPANT DRIFT MODEL

The memristor representing the physical model from [2], shown in fig. 2, consists of a bilayer thin film (size $D \approx 10\text{nm}$) of TiO_2 sandwiched between platinum contacts.

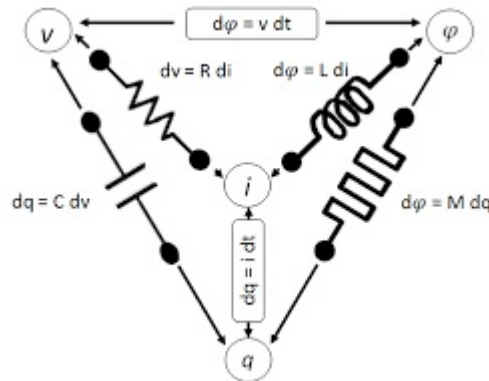


FIGURE 1. Indicates the missing gap in the passive elements now linked with the memristor.

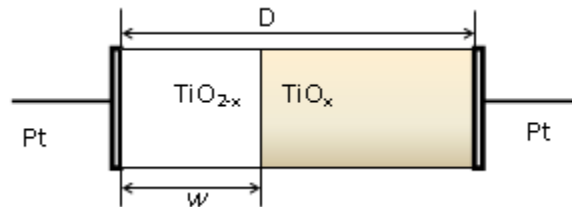


FIGURE 2. Bilayer structure of the memristor.

Where device structure having an 'D' bilayer thickness and width of doped region of 'w'. The electric field applied to the memristor in a given direction, the boundary between the two regions is moving in the same directions. The total resistance of the memristor, R_{MEM} , is the sum of the resistances of the doped and undoped regions,

$$R_{MEM}(x) = R_{ON}x + R_{OFF}(1-x), \tag{1}$$

$$\text{Where } x = \frac{w}{D} \in (0,1)$$

is the ratio of the width of the doped region, to the undoped region. (0 to D) represent doped area having the actual width of 'w', The relationship between the voltage and current of memristor ohm's law given by:

$$v(t) = R_{MEM}(w)i(t) \tag{2}$$

The rate at which the boundary movement between the doped and undoped regions depends on the resistance of doped area, on the passing current, and on other factors according to state equation[2].

$$\frac{dx}{dt} = ki(t)f(x), \quad k = \frac{\mu R_{ON}}{D^2} \tag{3}$$

Where $\mu \approx 10^{-14} \text{ m}^2 \text{ s}^{-1} \text{ V}^{-1}$ is the so-called dopant mobility. These smaller devices at nano size can yield enormous electric field even for small applied voltages,, which can secondarily produce significant nonlinearities in ionic transport. As a result, these can induce the rate at which the boundary between the doped to undoped regions gradually decreasing to zero. This phenomenon, called nonlinear dopant drift, can be modeled by the so-called window function $f(x)$ given in eqn.4. This paper uses the proposed window function in the following form:

$$f(x) = 1 - (2x-1)^{2p} \tag{4}$$

where p is a positive integer.

SPICE BASED SIMULATION RESULTS

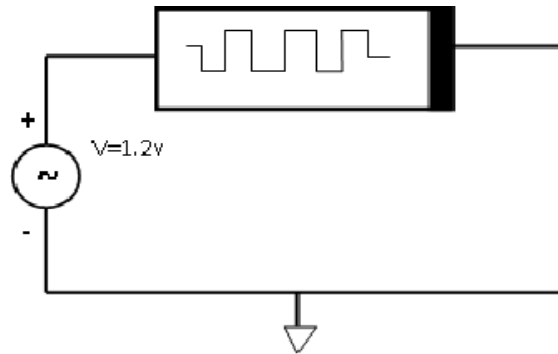


FIGURE 3. SPICE BASED MEMRISTOR CIRCUIT.

Cadence-OrCAD tool used to simulate this nonlinear ion-drift model[9]. The simulated results validate memristor’s internal characteristics such as pinched hysteresis loop, ϕ - q characteristics. Fig. 3 shows the SPICE based Memristor circuit. The memristor was excited with sinusoidal voltage amplitude of 1.2v and frequency of 1hz. Assumed $R_{init}=80k\Omega$, $R_{off}=100k\Omega$, $R_{on}=1k\Omega$ $\mu=10^{-14}m^2s^{-1}V^{-1}$, $p=1$ and $D=10nm$.

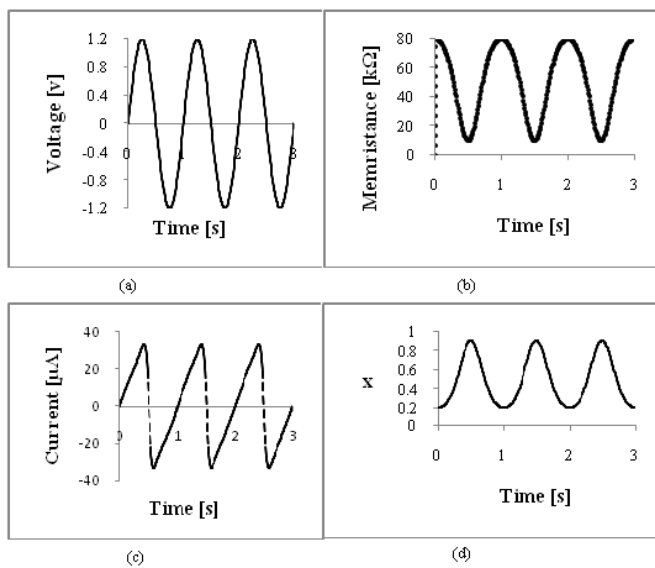
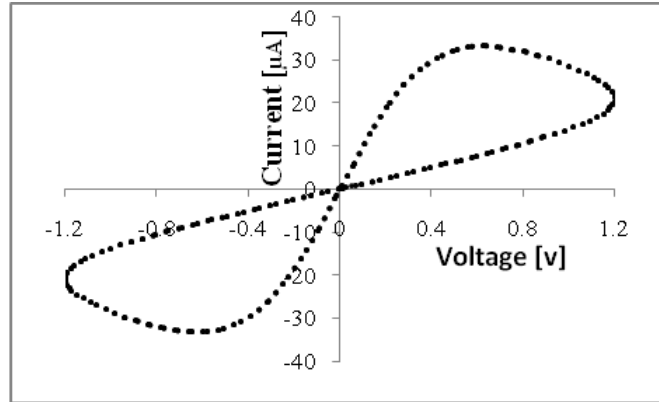


FIGURE 4.Simulation result analyses of memristor with respect to time(a) voltage (b) memristance (c) current (d) ratio of the width of the doped region to bilayer structure.

Figures 4(a-d) demonstrates the simulation result analyses of the memristor with respect to time. It can be inferred from the graphs the non-linearity of current with respect to time indicating the switching phenomenon (fig.4b). Also, the switching of memristance from high resistive state to low resistive in time fig.4c). Further, the normalized width x of the doped region is switched between the low and high levels near the limiting values of 0 and 1.

The typical memristor is shown in fig. 5. indicating a nonlinear curve with pinched hysteresis loop. The charge and flux relationship in fig. 6 confirm the time-domain integrals of electric current and voltage of the memristor confirming the well known fact that dependency between them inspite of the hysteresis effects.



FIGURES 5. i-v characteristics of Memristor.

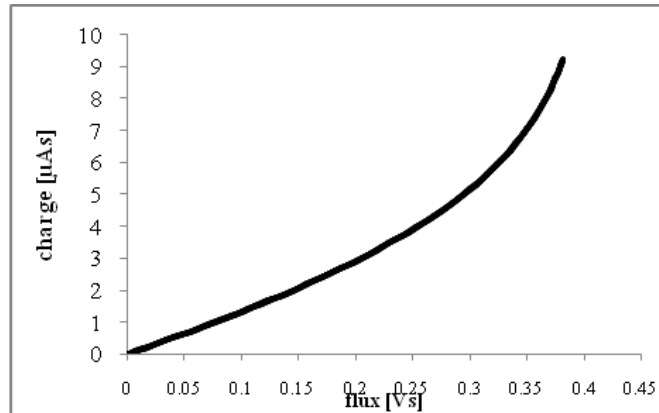


FIGURE 6. ϕ - q characteristics of Memristor.

RESULTS AND DISCUSSION

The effect on the frequency of the amplitude of the applied voltage, dopant mobility, applied voltage and thickness of the thin film layer affecting the non-linear i-v curve indicates the internal parameters of the simulated memristor which can aid in physical fabrication of memristor and simulating memristor based circuits.

A. Effect on the frequency of the applied voltage

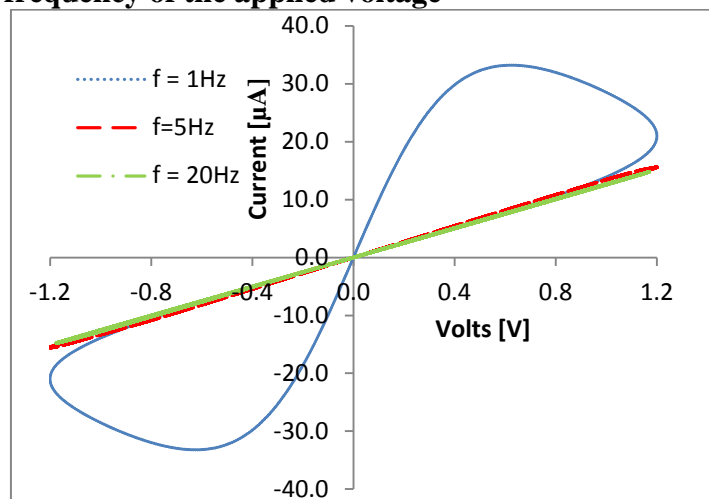


FIGURE 7. i-v characteristics for different frequencies.

In this simulation, the frequency is varied keeping the applied voltage 1.2v constant. It can be inferred from fig. 7. as frequency of the applied voltage increases the hysteresis double loop of non-linear curve diminishes and becomes a linear curve losing the memory effect.

B. Effect of the different excitation amplitude voltage

In this simulation experiment, different amplitude excitation voltage applied by keeping the frequency 1Hz constant. As shown in fig. 8. if the amplitude of the applied voltage increases the pinched hysteresis loops also increases and vice-versa. It has been observed that increasing the amplitude voltage of 2v at f=1hz results in hard threshold switching effects[10].

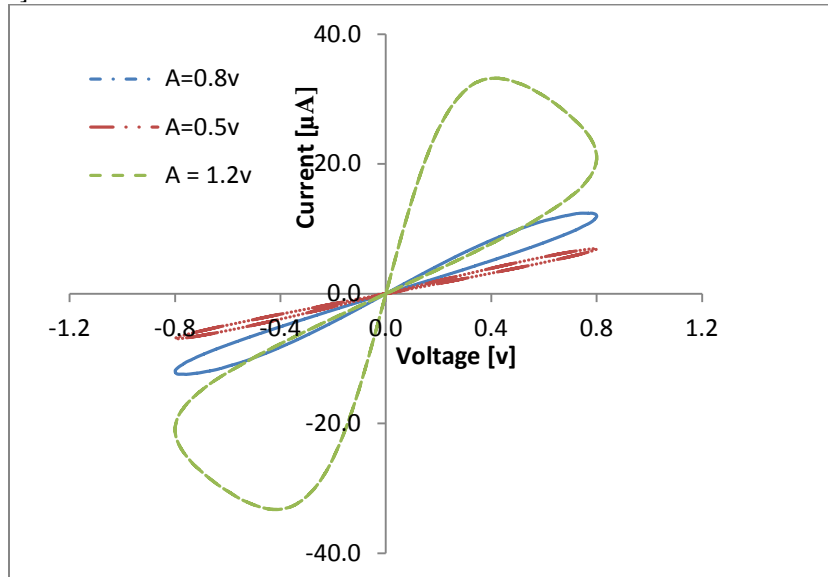


FIGURE 8. i-v curve for different amplitude of the applied voltage.

C. Effect of the thickness of the bilayer structure(D)

The simulation was carried with same amplitude voltage of 1.2v and frequency 1hz varying the bilayer thickness(D). When the thickness of the bilayer structure increased from 10nm to 100nm the non-linearity diminishes and becomes an linear curve as shown in fig. 9. The reason may be a high bias voltage is required because the distance of the doped region to cover the undoped area is larger. As a result threshold voltage of the device has not been exceeded resulting in an linear curve.

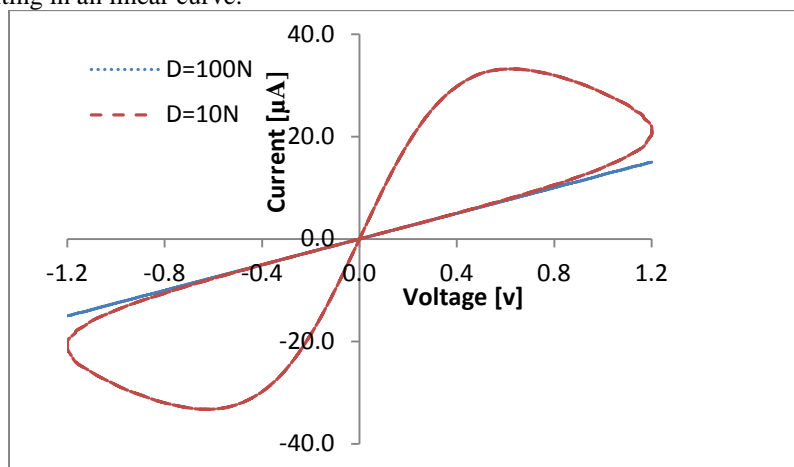


FIGURE 9. i-v curves for different thickness of bilayer structure.

D. Effect on the mobility of ions

The experiment was repeated having the same applied voltage 1.2v and frequency of 1hz but varying the mobility of dopant ions. Always higher the mobility of the so-called doped ions is preferred in order for the doped region to cross the boundary as early as possible. Hence, it is evident from the fig. 10. as the mobility of ions reduces the pinched hysteresis loop diminishes to a linear curve. Therefore the lower the mobility of the ions decreases ionic mobility hence, as the distance covered by the doped region is considerably less leading to an linear variation.

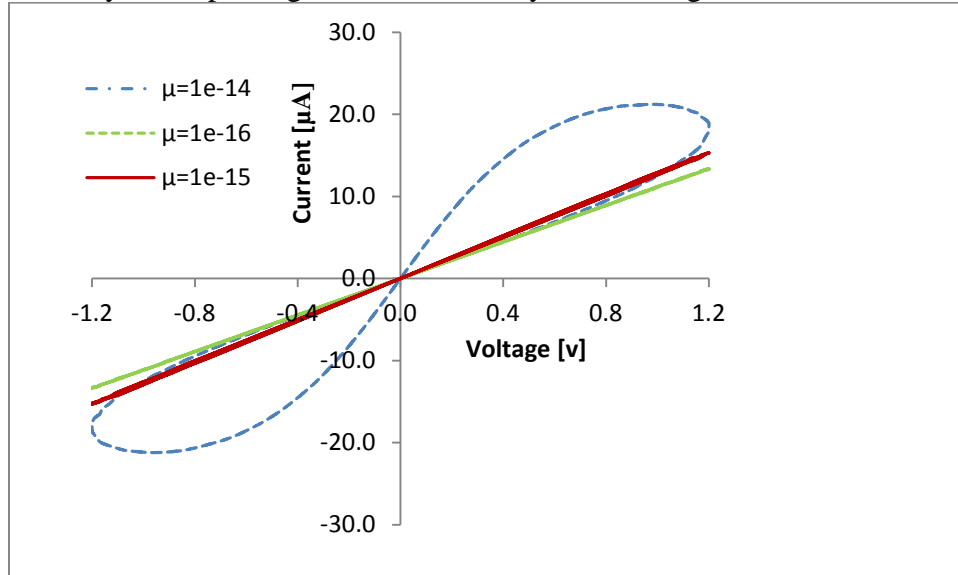


FIGURE 10. i-v curves for different values of mobility

E. Power dissipation

To implement synapse (to connect between two neurons) power consumption must be low. To simulate brain requires TB of computer memory, however with memristor low power consumption is possible[11]. It can be inferred that higher the pinched hysteresis loop can be obtained with increasing voltage with increasing frequency. Therefore an optimized voltage and frequency must be chosen to retain the large sized pinched hysteresis loop. In this simulation experiment, the power dissipation for the applied voltage of 1.2v and frequency 1hz was 28.798µW indicating better power dissipation phenomenon than the linear ion-drift model[12].

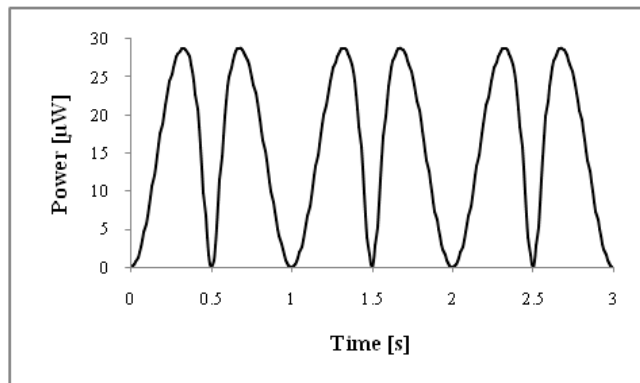


FIGURE 11. Power dissipation of memristor based on non-linear dopant drift model.

CONCLUSIONS

In this paper, characterization of memristor based on non-linear dopant drift model was simulated. This indicates simulated nonlinear ion drift model has better $v-i$ characteristics than linear ion-drift model. Also, the effect of changing values of frequency, applied voltage, thickness and mobility are studied. Furthermore, the results indicate that the suitability of memristor in neuromorphic system which requires high computer memory density with low power dissipation can be achieved.

REFERENCES

1. Chua, L.O., Memristor-the Missing Circuit element, IEEE Transactions on circuit theory, Vol.18, No.5, 507-519, (1971).
2. S.Prakash, S.Asokan, D.B.Ghare, A guideline for designing chalcogenide materials for threshold switching”, IEEE Transactions on Electronic device letters, vol.18, no.2, 45-47, (1997).
3. S.Prakash, S.Asokan, D.B.Ghare, Easily reversible memory switching, Journal of Physics D: Applied physics, vol.29, 2004-2008, (1996).
4. Strukov, D.B, Snider, G.S, Stewart, D.R, Williams, R.S. The missing memristor found, Nature, Volume No 453, 80-83, (2008).
5. Ioannis Vourkas, and Angel Abusleme, A Digital Memristor Emulator for FPGA-Based Artificial Neural Networks, 2016 1st IEEE International Verification and Security Workshop (IVSW).
6. Pershin, Y.V., DI Ventra, M., Practical approach to programmable analog circuits with memristors, IEEE Trans. Circ.Syst.I, Volume No 57, 1857,(2010).
7. Pershin, Y.V., DI Ventra, M., Memristive circuits simulate memcapitors and meminductors, IEEE Trans. Circ.Syst.I, Volume No 46, 517-518, (2010).
8. Manu Chilihuri, A high frequency memristor emulator circuit, M. Eng. thesis, University of Texas, Arlington, USA , Dec. 2015.
9. Biolek, Z., Biolek, D., Biolkova, V., SPICE model of memristor with nonlinear dopant drift, Radioengineering, vol.18, no.2, 210-214, (2009).
10. Pershin, Y.V., DI Ventra, M. SPICE model of memristive devices with threshold, Radioengineering, vol.18, no.2, 11-15, (2013).
11. Andy Thomas, Journal of Physics D: Appl., Phys., Vol. 46, 1-12, (2013).
12. T.V.Anusudha and S.R.S.Prabhakaran, Realization of non-linear I-V curve with low power dissipation using linear ion drift memristor model, IEEE ASQED 2015, 149-154.